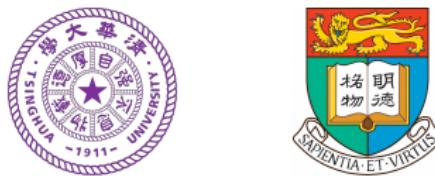


# A quantum experiment with joint exogeneity violation

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*Joint work with Dr. Xingjian Zhang from University of Hong Kong*



January 23, 2026

# Collaborators

Based on joint work with



Xingjian Zhang  
University of Hong Kong

# Acknowledgement

Quantum physicist:



Xiongfeng Ma  
Tsinghua University

Statistician:



Linbo Wang  
University of Toronto



Howard Wiseman  
Griffith University



Thomas Richardson  
U. of Washington

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- **marginal exogeneity**:  $Y(z) \perp\!\!\!\perp Z$  for  $z \in \{0, 1\}$ ;
- **joint exogeneity**:  $(Y(1), Y(0)) \perp\!\!\!\perp Z$ .

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## Talk overview

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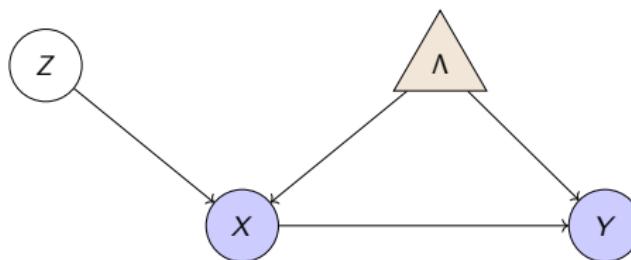
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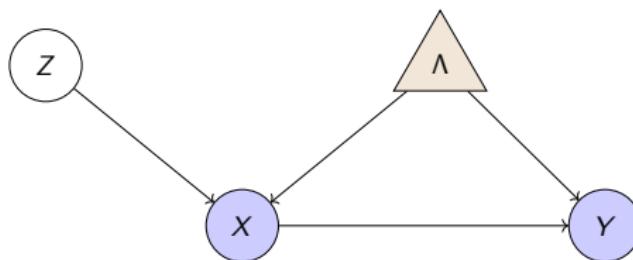
- We provide an example where assuming **joint exogeneity** of a fully randomized assignment results in a **contradiction** with other basic principles of causal models;
- We further discuss philosophical insights / open questions from this violation.

# Experiment: a randomized experiment with noncompliance



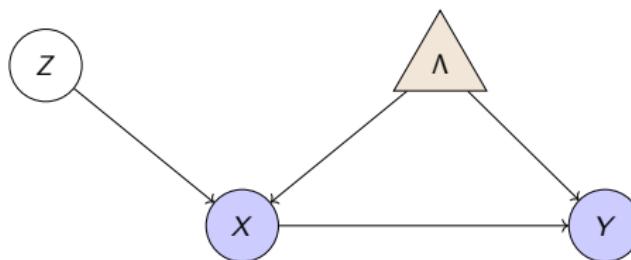
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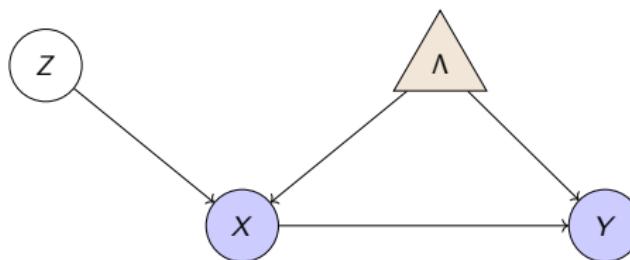
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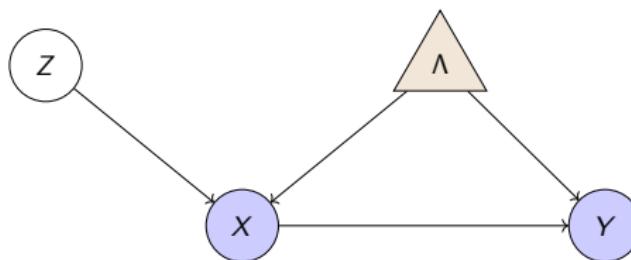
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⇒ **Ex:** adjusting the angle of **polarizer** based on the outputs.

## Theorem

Suppose we are under two assumptions:

- ① **existence of P.O.s:**  $Y(x, z)$  for  $x \in \{0, 1\}, z \in \{1, 2, 3\}$  exist;

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Then  $\mathcal{I}_Q := -\langle Y \rangle_1 + 2\langle Y \rangle_2 + \langle X \rangle_1 - \langle XY \rangle_1 + 2\langle XY \rangle_3 \leq 3$ , where

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This results in a **contradiction**:

- Chaves et al. (Nat. Phy. '18): there exists a quantum system constructed **according to** the IV graph s.t.  $\mathcal{I}_Q > 3$ .  
 $\Rightarrow$  It can be  $\mathcal{I}_Q = 1 + 2\sqrt{2}$ .

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  - Consistency
  - Intervention representability.

# Minimal requirements of P.O. existence

- Consistency:  $Y = \sum_{z \in \{1,2,3\}} \sum_{x \in \{0,1\}} \mathbb{1}\{\textcolor{blue}{X} = x, \textcolor{blue}{Z} = z\} Y(x, z);$

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Follows from exactly the same logic as def. of ATT / ATC:

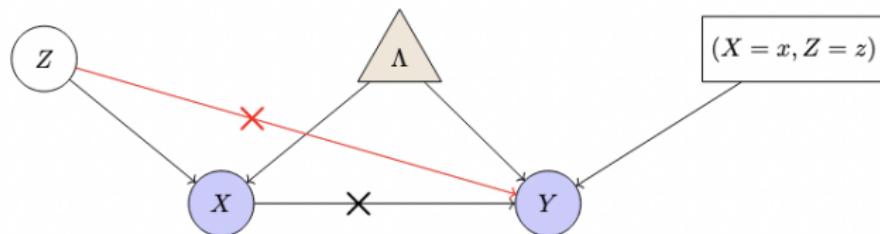
- $\mathbb{E}[Y(1) \mid T = 1] - \mathbb{E}[Y(0) \mid T = 1]$ ;
- or more generally:  $\mathbb{E}[Y(\textcolor{blue}{t}) \mid \textcolor{red}{T} = \textcolor{red}{t}']$ .

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Following **same logic** as ATT's def.,  $\mathbb{P}(Y(x, z) = y | X, Z)$

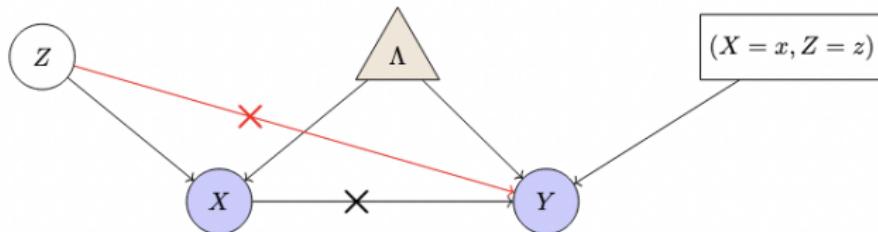
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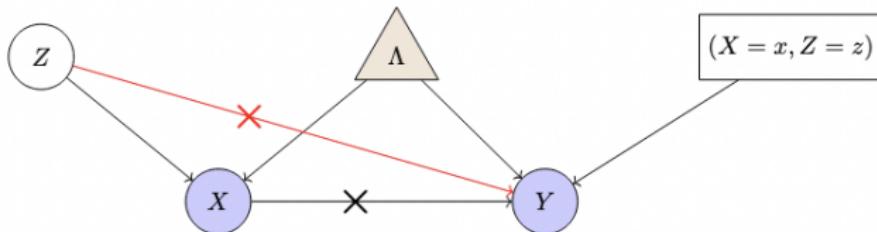


$$\mathbb{P}(Y(x, z) = y, X = x' | Z = z') = \text{tr}[(M_{x'}^{z'} \otimes N_y^x)\rho]$$

- $M_x^z, N_y^x \in \mathbb{H}^{2 \times 2}$ : specification of how the photons sent to  $X \& Y$  are **measured**;
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Proved that  $\mathcal{I}_Q \leq 3$ .

# Assumption summary

## Assumption 1

There exists random variables  $Y(0, 1), \dots, Y(1, 3)$  with

- (i) Consistency;
- (ii) Intervention representability.

## Assumption 2

Joint exogeneity

$$Z \perp\!\!\!\perp (Y(0, 1), \dots, Y(1, 3)).$$

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Consistency seems to be a fundamental assumption, so more likely:

joint exogeneity & intervention representability

**cannot** co-exist.

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# Discussions & Open questions

# Conditional interventional distribution

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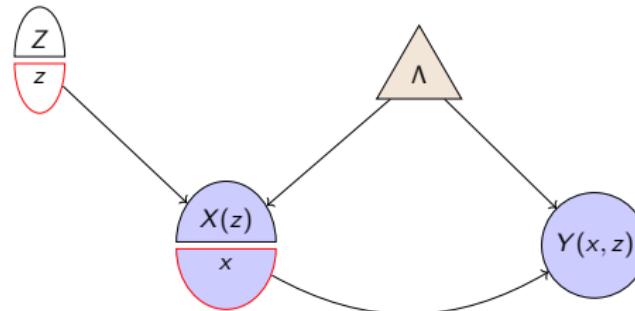
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- Not a “legal distribution” allowed by SWIG framework:



$\Rightarrow$  we can only define  $\mathbb{P}(Y(x, z) = y | X = x', Z = z')$

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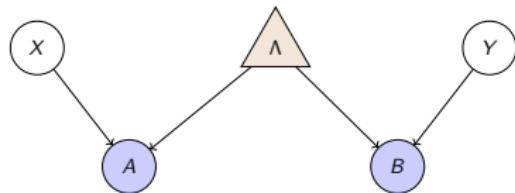
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- If not, does that mean P.O.s **cannot** model all ATT/ATC like queries?

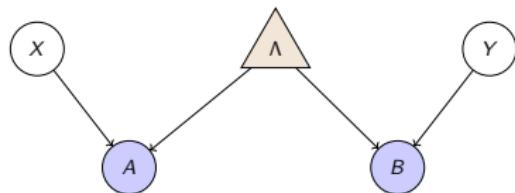
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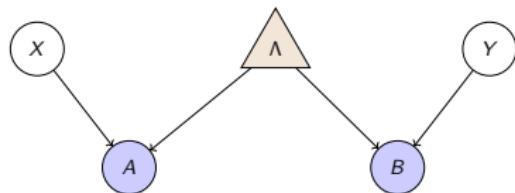
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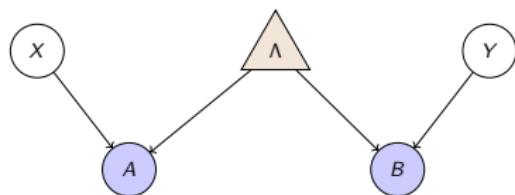
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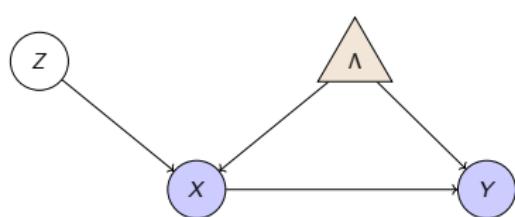
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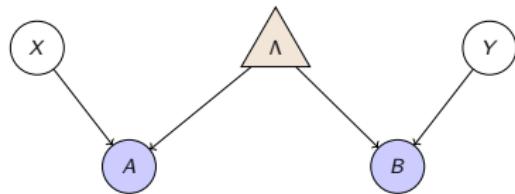


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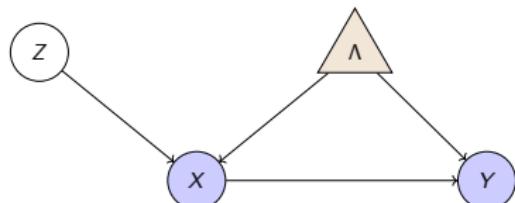
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- “locality” seems **not** assumed in our problem:

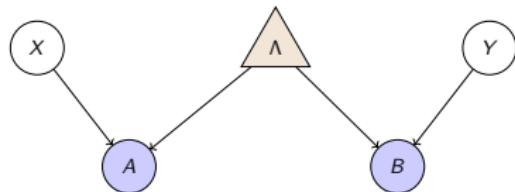
$$\mathbb{P}(Y(x, z_1) \neq Y(x, z_2)) > 0$$



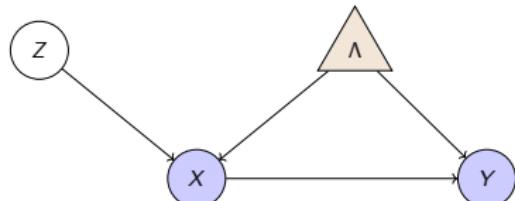
# Connections to Bell experiments

Showed the following three physical principles cannot coexist:

- Realism, freedom & locality;
- Assuming **any two** is still fine;
- Robins et al. (15), Gill (14): provided a P.O. definition of three principles.



Based on definitions from Robins et al. (15), Gill (14):



- “locality” seems **not** assumed in our problem:

$$\mathbb{P}(Y(x, z_1) \neq Y(x, z_2)) > 0$$

- **Q:** since we don't assume “locality”, why contradiction still exists?

# Discussion with quantum physcists / quantum logician

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## Open question:



**Howard Wiseman's conjecture:** “intervention representability” implicitly assumes certain kind of “locality”;  
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- ① How to rigorously justify this conjecture?



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~~> Different from Robins et al. (15), Gill (14): locality is not required if we just want to define P.O.s.

# Thank you for your attention!

Previous version (may be substantially revised based on feedbacks from open questions):

Wang, Y., & Zhang, X. (2025). *“A quantum experiment with joint exogeneity violation.”* arXiv:2507.22747